

1. What does it mean to say that a is a stationary point for a function f ? $f'(a) = 0$ (sec note 1 below)

2. Fact: if $f'(x) > 0$ on an interval (s, t) , then on that interval $f(x)$ is increasing.

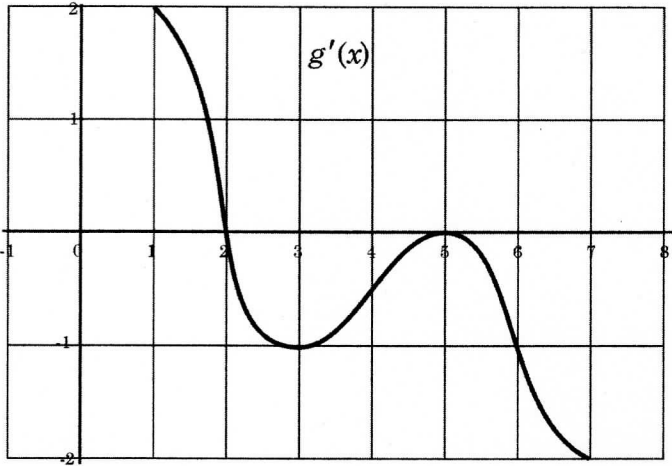
3. If a is a stationary point of f , then a is a local minimum point if f' changes from NEGATIVE to POSITIVE at a .
 (motivation: negative slopes to positive slopes)

(Possible answers might be "CU to CD" or "CD to CU" or "positive to negative" or "decreasing to increasing", etc).

4. An inflection point occurs at p if which function changes from increasing to decreasing at a : f , f' , or f'' ? f'

5. Consider the following graph of the derivative of function $g(x)$; so you are given the graph of $g'(x)$ here. Answer the following questions.

- (1) On what interval(s) is $g(x)$ decreasing? *if $g'(x) < 0$ on I then $g(x)$ is decreasing there so: $(2, 5)$ and $(5, 7)$ (sec note 2 below)*
- (2) What are the stationary points of $g(x)$? *$g'(a) = 0$ at $a = 2$ and $a = 5$*
- (3) On what interval(s) is $g(x)$ concave down? *if g' is decreasing on I , then g is C.D. there, so $(1, 3)$ and $(5, 7)$*
- (4) Does $g(x)$ have any local maximum points or minimum points? If so, list their x -coordinates and classify them (local min or local max). *at $a = 2$, g' changes from POS to NEG, so g changes from incr to decr \Rightarrow there is a local MAX at $a = 2$.*
- (5) Find all the inflection points of $g(x)$. *at each of $a = 3$ and $a = 5$, g' changes from decr to incr OR incr to decr so g changes from CD to CU OR CU to CD; in either case the point is an I.P.*
- (6) Make a rough sketch of g on the bottom graph starting at the dot given. Make sure it increases/decreases and is CD/CU where it should be; but you do not need to worry about the location of the x axis.



decr to incr
 OR
 incr to decr so
 g changes from CD to CU
 OR
 CU to CD; in either case
 the point is an I.P.

note 1: if you want to talk about tangent lines, you need to say:
 "the slope of the line tangent to the graph of f at $(a, f(a))$ is 0"

note 2: will accept $(2, 7)$ also.

