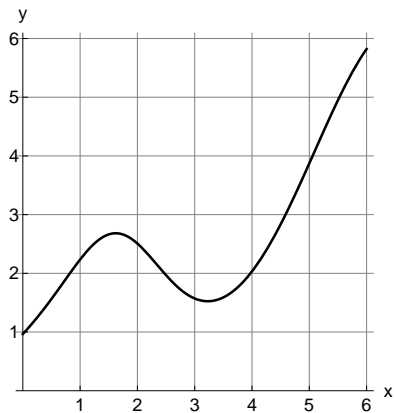


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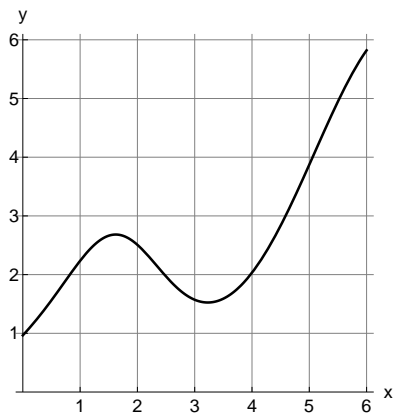
YOUR GRADE IS BASED ON CORRECTNESS, COMPLETENESS, AND CLARITY ON EACH EXERCISE. EXPLAIN ALL ANSWERS COMPLETELY. YOU MAY USE A CALCULATOR, BUT NO NOTES, BOOKS, OR OTHER STUDENTS. GOOD LUCK!

1.) (10 pts.) Use the given graphs to compute L_3 and T_3 . Simplify your answers.

a.) (5 pts.) On the graph below, sketch in and compute L_3 .



b.) (5 pts.) On the graph below, sketch in and compute T_3 .



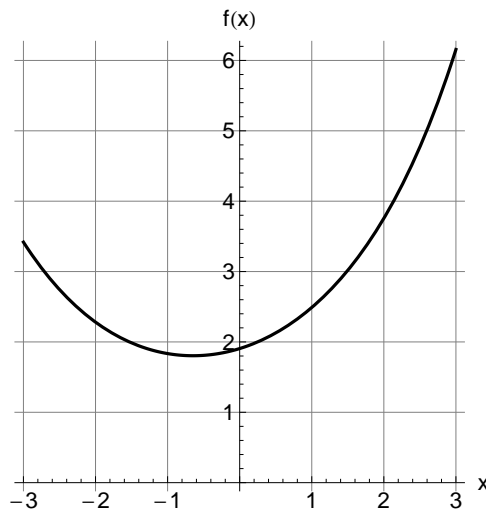
2.) (15 pts.) This problem combines our three big calculus concepts: the integral, the derivative, and the limit.

a.) (5 pts.) Use the Fundamental Theorem of Calculus to compute $\int_{\frac{1}{2}}^1 (x^{-3} - 8) dx$.

b.) (5 pts.) Compute the derivative of $y = x^{-3} - 8$.

c.) (5 pts.) Compute the limit $\lim_{x \rightarrow 0} (x^{-3} - 8)$. Be sure to demonstrate how you are computing the limit.

- 3.) (15 pts.) The equation $f(x) = \frac{\pi}{e} + 2^{x-1} + \frac{x^2 + 2}{x + 8}$ is shown in the graph below.



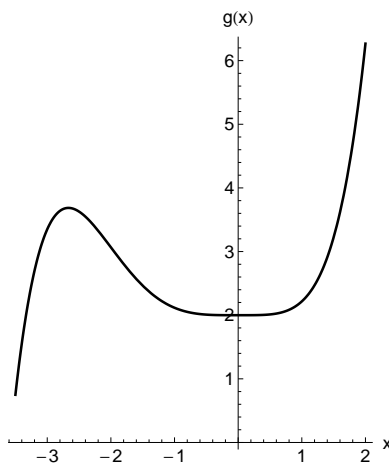
- a.) (5 pts.) Use the graph to *visually approximate* $f'(2)$.
- b.) (5 pts.) Use the given equation to compute $f'(x)$.
- c.) (5 pts.) Use your result from part (b) to compute an exact value for $f'(2)$. Compare the decimal approximation of your exact answer with your answer from part (a): how close were you?

4.) (15 pts.) The following are two examples of techniques we have learned that require multiple steps.

a.) (7 pts.) Use L'Hôpital's Rule to compute $\lim_{x \rightarrow 0} \frac{1 - \cos(3x)}{8x}$. Be sure to confirm why you *can* use L'Hôpital's Rule.

c.) (8 pts.) Use implicit differentiation to compute $\frac{dy}{dx}$ for the equation $2(x + y)^{\frac{1}{3}} = y$. Be sure to solve for $\frac{dy}{dx}$.

- 5.) (15 pts.) The function $g(x) = \frac{1}{20}x^5 + \frac{1}{6}x^4 + 2$ is shown in the graph below. You may choose to answer part (a) first, or wait and use your results from parts (b) and (c).



- a.) (5 pts.) State the x -intervals for which the following hold. You can restrict $g(x)$ to the x -values $[-3.5, 2]$, as shown in the graph.
- $g(x)$ is increasing
 - $g(x)$ is decreasing
 - $g(x)$ is concave up
 - $g(x)$ is concave down
- b.) (5 pts.) Use calculus to show how you know the exact x -values at which stationary points occur.
- c.) (5 pts.) Use calculus to find any inflection points and confirm that they are inflection points.

- 6.) (15 pts.) The following all relate to theorems we have discussed this semester.
- a.) (5 pts.) The theorem we have nicknamed the “Trick Question Theorem” says *either* “if a function is continuous, then it must be differentiable” *or* “if a function is differentiable, then it must be continuous”. Which of these is correct, and what example reminds us that the other one is not correct?
- b.) (5 pts.) State the hypotheses of the Mean Value Theorem.
- c.) (5 pts.) State the conclusion of the Mean Value Theorem, and use a graph to explain visually what the formula means.

7.) (15 pts.) A rectangle initially has dimensions 2 cm by 4 cm. All sides begin increasing in length at a rate of 1 cm/s. At what rate is the area of the rectangle increasing after 20 s?

BONUS: (5 pts.) Many of you have already done this, but in case you have not yet: by 4:00pm today (Tuesday, April 10) email me a photo of yourself at the Mount David Summit.