

Name: KEY

Show all work, clearly and legibly, to receive full credit. Correct spelling, organization of your solution, and proper use of mathematical notation all count. You may use a stand-alone graphing calculator, but not any internet-based calculators. No notes, books, or other additional resources are permitted. Good luck!

1.) (4 pts.) Compute $f'(x)$ if $f(x) = 4^{\sqrt{\ln x}}$. Do not simplify your answer.

$$f'(x) = 4^{\sqrt{\ln x}} \cdot \ln 4 \cdot \frac{1}{2} (\ln x)^{-\frac{1}{2}} \cdot \frac{1}{x}$$

2.) (4 pts.) Evaluate the limit, showing how you do so:

$$\begin{aligned} 1) &= \lim_{t \rightarrow \infty} \frac{2t+3}{5-4t} \cdot \frac{t}{t} \\ &= \lim_{t \rightarrow \infty} \frac{2 + \frac{3}{t}}{\frac{5}{t} - 4} \rightarrow 0 \\ &= \frac{2}{-4} \\ &= \left(-\frac{1}{2} \right) \end{aligned}$$

$$\lim_{t \rightarrow \infty} \frac{2t+3}{5-4t}$$

2.) Ratio of coefficients
 $\frac{2}{-4} = -\frac{1}{2}$
 because the highest power of t , top and bottom, is the same.

3.) Graph or L'Hopital's Ru
 since, as $t \rightarrow \infty$:
 $2t+3 \rightarrow \infty$ and
 $5-4t \rightarrow -\infty$ then
 $\lim_{t \rightarrow \infty} \frac{2}{-4} = \left(-\frac{1}{2} \right)$

3.) (2 pts.) Simplify $\log_4(1/16)$. Your answer should be a number and should not involve a logarithm.

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