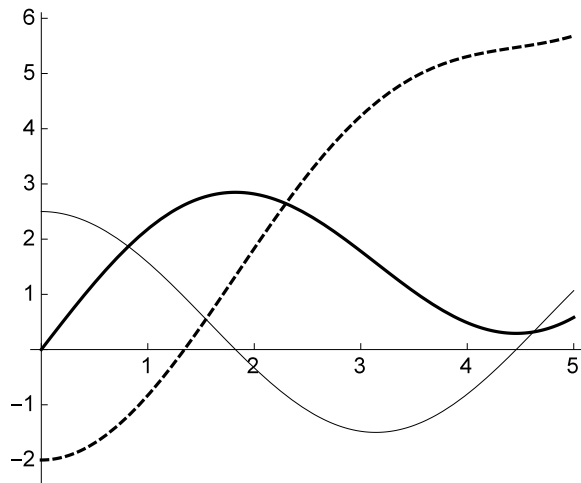


Name: _____

SHOW ALL WORK, CLEARLY AND LEGIBLY, TO RECEIVE FULL CREDIT. CORRECT SPELLING, ORGANIZATION OF YOUR SOLUTION, AND PROPER USE OF MATHEMATICAL NOTATION ALL COUNT. YOU MAY USE A STAND-ALONE GRAPHING CALCULATOR, BUT NOT ANY INTERNET-BASED CALCULATORS. NO NOTES, BOOKS, OR OTHER ADDITIONAL RESOURCES ARE PERMITTED. GOOD LUCK!

1.) (10 pts.) The graphs below are f , f' , and f'' . State which is which, and explain how you know this.



2.) (15 pts.)

a.) (5 pts.) Suppose $\lim_{x \rightarrow 5^-} f(x) = 2$ and $\lim_{x \rightarrow 5^+} f(x) = 4$. Is it possible that $\lim_{x \rightarrow 5} f(x) = 3$? Justify your answer.

b.) (5 pts.) Suppose $g(x) = \frac{x^2 + 3x - 10}{x - 2}$. What is $g(2)$? [Note: $g(x)$ is not related to $f(x)$ in part (a).]

c.) (5 pts.) What is $\lim_{x \rightarrow 2} \frac{x^2 + 3x - 10}{x - 2}$?

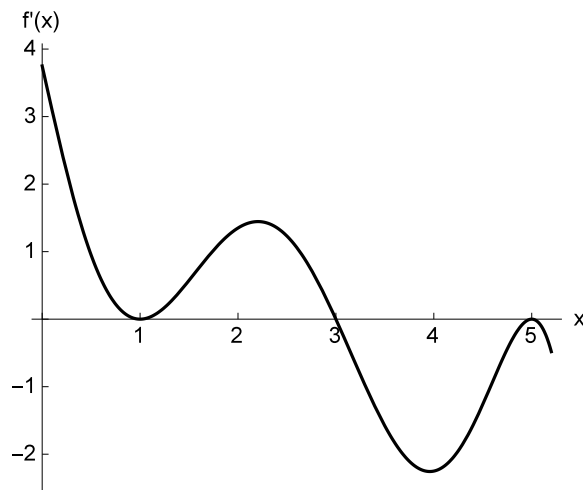
3.) (15 pts.)

a.) (5 pts.) Give an example of a polynomial, and describe in words what it means for a function to be a polynomial.

b.) (5 pts.) Give an example of a rational function, and describe in words what it means for a function to be a rational function.

c.) (5 pts.) Give an example of an exponential function, and describe in words what it means for a function to be an exponential function.

4.) (15 pts.) Shown below is a graph of f' on its entire domain. The graph is NOT f .



a.) (3 pts.) At which x -value(s) does f have a stationary point?

b.) (3 pts.) At which x -value(s) does f' have a stationary point?

c.) (3 pts.) At which x -value(s) is f greatest?

d.) (3 pts.) At which x -value(s) is f increasing?

e.) (3 pts.) At which x -value(s) is f concave up?

5.) (15 pts.) For each of the following questions, let $f(x) = \sqrt{x} + \frac{1}{x^3}$. On this page, you may complete the exercises using the Power Rule we learned for computing derivatives and antiderivatives.

a.) (5 pts.) Compute the general antiderivative $F(x)$.

b.) (5 pts.) Solve the initial value problem in which the differential equation is $f(x)$ and the initial condition is $F(1) = 3$.

c.) (5 pts.) Compute $f'(x)$.

6.) (15 pts.) Consider the function $f(x) = \ln(8x)$.

a.) (5 pts.) Draw $f(x)$, showing the graph for x -values ranging from 0 to 5.

b.) (5 pts.) Numerically zoom to estimate $f'(2)$.

c.) (5 pts.) Explain, referring to your graph, how the idea of numerical zooming leads us to the exact definition of the derivative at a point (such as at the point $x = 2$).

7.) (15 pts.) Use **the limit definition of the derivative** to compute $f'(x)$ for $f(x) = 3x^2 + 5x$. [NOTE: you may use the Power Rule to check your result, but that alone will earn you no credit.]