

Math 105 Quiz 1

§1.1-§1.4

Name: *Key*

Show all work for credit.

1. Give the domain and range of the following functions (Hint: They should not be the same):

(a)  $f(x) = x$   
 $D: (-\infty, \infty)$ , all reals  
 $R: (-\infty, \infty)$ , all reals

(b)  $g(x) = (\sqrt{x})^2$   
 Note  $\sqrt{x}$  requires  $x \geq 0$   
 $D: [0, \infty)$ ,  $x \geq 0$   
 $R: [0, \infty)$ ,  $y \geq 0$

(c)  $h(x) = \frac{1}{x^2}$   
 Note division by  $x$  means  $x \neq 0$   
 $D: (-\infty, 0) \cup (0, \infty)$ , all reals except 0  
 $R: (-\infty, 0) \cup (0, \infty)$ , all reals except 0

2. The graph of  $j$  can be found from the graph of  $k$  if you:

- (a) Shift  $k$  left 2 units then  $k(x+2)$   
 (b) Flip over the  $x$ -axis then  $-k(x+2)$   
 (c) Shift down by 3 units.  $-k(x+2) - 3$

Write the function  $j(x)$  based on  $k(x)$ . i.e.  $j(x) = 2k(x-5) - 1$  (this is NOT the answer, but here to give you an example).

$$j(x) = -k(x+2) - 3$$

3. What is the working definition of  $f'$ , the derivative of some function  $f$ ?

$f'$  is the <sup>function of</sup> instantaneous rate of change of  $f$   
 $f'(a)$ : slope of the tangent line through  $(a, f(a))$   
 $f'(a)$ : slope at  $(a, f(a))$  on  $f$